In mid-May 1950, just 59 years ago, we met in Sarov. Next 4 years, 1 worked by him ...



Symmetry Breaking at Phase Transitions

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What is the Symmetry that breaks at Phase Transition ?



Motivation

- Spontaneous Symmetry Breaking;
 From magnetics to Quantum Statistics
- Broken Symmetries in Quantum Field Theory and ... Nobel Prize in Physics 2008

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- What is the (broken) Symmetry
 - of a physical system ?
 - of the physical problem ?

Phase transition and broken symmetry

Connection btwn Phase transition and symmetry breaking was evident before the QM creation –> e.g., from physics of crystals Landau 1937 theory of phase transitions :

starts with Introduction in Symmetries,

Phase transition and broken symmetry

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Landau 1937 theory of phase transitions :

- starts with Introduction in Symmetries,
- but, only discrete symmetries :
- on SuperFluidity "He II is not a liquid crystal !"

Meanwhile, Landau's "Mechanics" (1937/40) is based upon continuous symmetries, invariance and conservation laws.

Symmetries and groups

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Quantum Symmetries :

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 Non-relativistic 2nd-quantized neutral field Phase transformation= a → e^{-iα} a, a* → e^{iα} a* -> N = const. Conserving Number of particles
 Charged (2-, 3-component) field; Gauge=phase transformation -> Current; Charge conservation

Quantum Symmetries

Qu-Symmetries: Phase, Gauge, Chiral, SuSy, Qu-Symmetries are quite different from "Classical" ones, like spatial (boosts, rotations, Lorentz) and internal (isospin, flavor) ones.

For their formulation and understanding one has to use quantum notions :

- * unobservability of the ψ -function phase;
- * spin, chirality;
- * difference btwn Bose- and Fermi-statistics.

Bogoliubov model for SF He II

Bogoliubov 1946 microscopic theory – non-ideal $H_{\rm B-gas} = \sum_{\vec{p}} \frac{p^2}{2m} a_p^+ a_p + \frac{1}{2V} \sum v(p_1 - p_2) a_{p_1}^+ a_{p_2}^+ a_{p_2} a_{p_1};$

Bose gas with weak repulsion v(p) > 0.

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The Hamiltonian has $[a \rightarrow e^{-i\alpha}a, a^* \rightarrow e^{i\alpha}a^* =]$ phase symmetry -> No of particles conservation, as $H_{\text{B-gas}}$ commutes with $\mathbf{N} = \sum_{\vec{p}} a_p^+ a_p$

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Bogoliubov's physical hypothesis:

"macroscopic condensate"

$$\mathbf{N}_{\mathbf{p}=\mathbf{0}} = \mathbf{a}_{\mathbf{0}}^+ \, \mathbf{a}_{\mathbf{0}} \sim \mathbf{N}_{\mathbf{A}}$$

Corollary: condensate operators $a_0^+, a_0 \sim \sqrt{N_0} = c$ -numbers

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Bogoliubov SuperFlu model

Shift $\psi(\mathbf{x}) = \Psi_0 + \phi(\mathbf{x})$ by "big" constant $\Psi_0 \sim \sqrt{N_0}$ results in bilinear approximate Hamiltonian

$$\mathbf{H}_{\mathbf{Bog}} = \sum_{\mathbf{p}\neq\mathbf{0}} \left(\frac{\mathbf{p}^2}{2\mathbf{m}} + \frac{\mathbf{N}_0}{\mathbf{V}} \mathbf{v}(\mathbf{p}) \right) \mathbf{b}_{\mathbf{p}}^+ \mathbf{b}_{\mathbf{p}}, \ + \ \frac{N_0}{2V} \sum_{p\neq0} v(p) [b_p^+ b_{-p}^+ + b_p b_{-p}]$$

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$$\begin{split} \mathbf{H}_{\mathbf{Bog}} &= \sum_{\mathbf{p} \neq \mathbf{0}} \left(\frac{\mathbf{p}^2}{2\mathbf{m}} + \frac{\mathbf{N}_0}{\mathbf{V}} \mathbf{v}(\mathbf{p}) \right) \mathbf{b}_{\mathbf{p}}^+ \mathbf{b}_{\mathbf{p}}, \ + \frac{N_0}{2V} \sum_{p \neq 0} v(p) [b_p^+ b_{-p}^+ + b_p b_{-p}] \\ \text{with } b_p^+, \ b_p - \text{``above-condensate''} \ \text{Bose-operators.} \\ \mathbf{H}_{\mathrm{Bog}} \ \text{describes creation of pairs of Helium atoms} \\ \text{with opposite momenta from condensate and their} \\ \text{``annihilation''} \ \text{into condensate.} \\ \text{Interaction btwn pairs is small} \sim N_0^{-1/2} \ \text{and omitted.} \end{split}$$

Total No of these correlated pairs is not fixed.

Symmetry of Bogoliubov SF model

$$H_{\text{Bog}} = \sum_{p \neq 0} \left(\frac{p^2}{2m} + \frac{N_0}{V} v(p) \right) b_p^+ b_p + \frac{N_0}{2V} \sum_{p \neq 0} v(p) \left[b_p^+ b_{-p}^+ + b_p b_{-p} \right]$$

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Violates phase invariance

$$b \to e^{-i\phi} b \,, \, b^+ \to e^{i\phi} b^+$$

due to non-conservation of number of above-condensate particles (responsible for the phase transition);

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Diagonalized by Bogoliubov (u, v) transformation

$$\xi_p = u_p b_p + v_p b_{-p}^+ = U_\alpha^{-1} b_p U_\alpha; \quad \xi_p^+ = u_p b_p^+ + v_p b_{-p}.$$

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New ground state and its exitations, like

$$\Psi_0^{\text{Bog}} \sim e^{\sum_p \alpha(p) \, b_p^+ b_{-p}^+} \, \Psi_0; \ \Psi_1^{\text{Bog}}(k) = \xi_k^+ \, \Psi_0^{\text{Bog}}$$

contain superposition of indefinite number of He II atom pairs with opposite momenta.

Bogoliubov – Landau spectrum *

Resulting Hamiltonian

$$H = E_0 + \sum_{p \neq 0} E(p) \,\xi_p^+ \,\xi_p \,, \quad E(p) = \sqrt{\left(\frac{p^2}{2m}\right)^2 + \frac{p^2}{2m}} \,v(p)$$

describes collective excitations = coherent

superposition of correlated pairs with total zero mom.

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$$E(p \rightarrow 0) = c p; \ c = \sqrt{\frac{v(0)}{m}}$$

like, e.g. $v(p) \sim \frac{sin(a p)}{a p}$

The spectrum joints phonons and "rotons".

Phase symmetry breaking in SF state

Initial Hamiltonian $H_{B-g}(a_p^+, a_p)$ for normal states $\langle a_p \rangle = 0$ is invariant with respect to the

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The bilinear Bog's model Hamiltonian $H_{\text{Bog}}(b_p^+, b_p)$, as well as the (u, v) canonical transformation, is not compatible with PhT. Physically, this corresponds to non-conserved number of relevant above-condensate particles.

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Symmetry in SuperConductivity ?

- Along with S.Weinberg (2007) :
- "BCS SuperCond \rightarrow Gauge symmetry \rightarrow Charge conserving violated."
- Which Symmetry is Broken indeed in SC?
- 1. In Ginzburg-Landau (1950) phenomenological theory ? :

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- 1. In Ginzburg-Landau (1950) phenomenological theory ? :
- There, $\Psi(r)$ effective classic function =
- 2-component order parameter $\Psi(r) = |\Psi(r)|e^{i\Phi(r)}$ entering free energy functional

$$F = F_n + \int \left(\frac{\hbar}{2m^*} |\vec{\nabla}\Psi(r)|^2 + A |\Psi(r)|^2 + b |\Psi(r)|^4\right) dV$$

with $A \sim T - T_c$, changing sign at $T = T_c$
(and b, m^* – not depending on temperature T .)

Ginzburg-Landau [1950] Macro SuperConductivity

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Effective potential $V(|\Psi|) = A |\Psi|^2 + b |\Psi|^4$. corresponds to Fig.1. The G-L Symmetry is like of the Champagne bottle with convex bottom

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Symmetry in BCS+Bogoliubov SC

What symmetry is broken in BCS+Bogoliubov SC? (not Gauge one, related to Electric charge conservation !)

to Remind :

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 Symmetry in Bog's SuperFlu = Phase factor Symm.
 SSB related to non-conservation of correlated pairs of He II atoms responsible for Phenomenon

to Announce :

- In BCS and Bog's it's broken Phase Symmetry
- In BCS non-phase-symm trial ψ_{BCS} function.
- broken Phase Symmetry in Bog's SC due to non-conservation of Cooper pairs No.

BSC SuperConductivity

BCS model: $H = T + H_{BCS}$ $H = \sum_{\vec{k},\sigma} \varepsilon_{\vec{k}} c^+_{\vec{k}\sigma} c_{\vec{k}\sigma} + \sum_{\vec{k},\vec{k}'} V_{\vec{k},\vec{k}'} c^+_{\vec{k}\uparrow} c^+_{-\vec{k}\downarrow} c_{-\vec{k}'\downarrow} c_{\vec{k}'\uparrow},$ - eff. Cooper pairs (antipodes) attraction $\varepsilon_{\vec{k}} = \frac{\vec{k}^2}{2m} - \varepsilon_F$ - electron energy above ε_F



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Effective electron attraction in the vicinity of Fermi surface

$$V(\vec{k}, \vec{k}') = \begin{cases} -V_C, & |\varepsilon_{\vec{k}} - \varepsilon_{\vec{k}'}| < \omega_{ph} \\ 0, & |\varepsilon_{\vec{k}} - \varepsilon_{\vec{k}'}| > \omega_{ph} \end{cases}$$



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Trial BCS function $\Phi_0^{BCS} = \prod_{\vec{k},\sigma} \left(u_k + \sqrt{1 - u_k^2 c_{\vec{k}\uparrow}^+ c_{-\vec{k}\downarrow}^+} \right) \Psi_0$ with Cooper pairs

BSC SuperConductivity: 3 comments

1. In the position space, H_{BCS} corresponds to factorizable expression

$$H_{BCS} = \int dx C^+(x) C^+(x) V_{BCS} \int dy C(y) C(y)$$

There is no (x - y) dependence in the kernel V_{BCS} ; phonon from diagram does not transfer the momentum. As it was well-known, this destroys the current continuity.



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3. G-L order parameter

$$\Psi(\mathbf{k}) = \langle c^{\dagger}_{\mathbf{k}\uparrow} c^{\dagger}_{-\mathbf{k}\downarrow} \rangle$$

Gor'kov - '59

Bogoliubov micro SC theory

Fröhlich electron-phonon model: $H_{Fr} =$ $= \sum_{\vec{k},\sigma} \varepsilon_{\vec{k}} c^+_{\vec{k}\sigma} c_{\vec{k}\sigma} + \sum_{\vec{q}} \omega_{\vec{q}} b^+_{\vec{q}} b_{\vec{q}} + g_{Fr} \sum_{\vec{k},\vec{k}',\sigma} \sqrt{\frac{\omega(\vec{q})}{2V}} c^+_{\vec{k}\sigma} c_{\vec{k}'\sigma} (b^+_{\vec{q}} + b_{-\vec{q}})$ Bogoliubov (u,v) transformation: $\alpha_{\vec{k}\uparrow} = u_{\vec{k}} c_{\vec{k}\uparrow} - v_{\vec{k}} c^+_{-\vec{k}\downarrow}; \quad \alpha_{\vec{k}\downarrow} = u_{\vec{k}} c_{\vec{k}\downarrow} + v_{\vec{k}} c_{-\vec{k}\uparrow^+} \quad (u-v)$ violates phase symmetry

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$$H_{Fr} \to H_B = \sum E_{\vec{k}} \; \alpha^+_{\vec{k},\sigma} \; \alpha_{\vec{k},\sigma}$$

$$E_{\vec{k}} = \sqrt{\varepsilon_{\vec{k}}^2 + |\bigtriangleup_{\vec{k}}|^2}$$

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Spectrum with gap; Bogolon dissociation *

To elucidate Bogolon's physical content, take spectral function of quasiparticle excitations in SC phase

$$A_{sc}(\mathbf{k},\omega) = u_{\mathbf{k}}^2 \,\delta(\omega - E_{\mathbf{k}}) + v_{\mathbf{k}}^2 \,\delta(\omega + E_{\mathbf{k}}),\tag{1}$$

as in the Figure

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as in the Figure



Spectral function of 1-electron quasipartical exitations in Bog's theory



Different Symmetries in Macro- and Micro-

Thus, the Broken Symmetry of microtheory of SuperConductivity (like in Bog's SuperFluidity) – is the phase Symmetry., Nonconservation of the No of Cooper pairs or He II atoms relevant for the phase transition. Different Symmetries in Macro- and Micro-

Thus, the Broken Symmetry of microtheory of SuperConductivity (like in Bog's SuperFluidity) – is the phase Symmetry., Nonconservation of the No of Cooper pairs or He II atoms relevant for the phase transition. Compare with Champagne bottle Symmetry of macrophenomenological Ginzburg-Landau theory. Micro and Macro Symmetries are different **Essentially different** !

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- Symmetry of Quantum Problem (operator eq., eigenvectors and matrix elements); of Approximation to Qu-Problem.
- * Do they relate to Symmetry of physical system ?

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- <u>Classical</u> (obvious) Symmetries: in crystals;
- <u>"Intermediate</u>" Symmetries

- artificial but scenically transparent -

{in order-parameter phenomenology macromodels}, Champagne-bottle = Mexican hat;

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- Among Qu-Sym, approximate (in pQCD)

Modern Pilatus vs Critical phenomena

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"What is the Verity?" = that's the old question.

The new one :

What is the Symmetry?

Pilatus

"Quid est symmetria ?"

